

# Correlation models for next-generation amplitude and cumulative intensity measures using artificial neural networks

*Savvinos Aristeidou<sup>1</sup>*, *Davit Shahnazaryan<sup>2</sup>*, *Gerard J. O'Reilly<sup>3</sup>*

*1 – PhD candidate, IUSS Pavia, Italy*

*2 – Postdoctoral Researcher, IUSS Pavia, Italy*

*3 – Associate Professor, IUSS Pavia, Italy*



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# Introduction

- Plethora of intensity measures (IMs) to characterise the intensity of a ground motion
  - Traditionally, only  $Sa$  is explicitly considered in seismic risk analyses
  - Filtered incremental velocity,  $FIV3$ , was shown to be an excellent IM in predicting the collapse of structures
  - Average spectral acceleration,  $Sa_{avg}$ , was shown to be well-correlated with a wide range of structural response
  - Significant duration,  $Ds$ , was found to influence the structural damage due to cumulative effects
- Correlation models between a few aforementioned IMs are still missing from the literature
- Required for vector-based PSHA and ground motion record selection (e.g., GCIM method).
- Predictive models of the empirical correlation coefficients were developed using artificial neural networks (ANNs)

# Correlation models developed (IM pairs)

- ***PGA***: peak ground acceleration
- ***PGV***: peak ground velocity
- ***Sa(T)***: 5%-damped spectral acceleration at a vibration period,  $T$ . Period range: 0.01 s to 5 s
- ***Ds<sub>xy</sub>***: x-y% significant duration. The proposed models include  $\{x, y\} = \{5\%, 75\%\}$  and  $\{x, y\} = \{5\%, 95\%\}$
- ***Sa<sub>avg</sub>(T)***: average spectral acceleration, for two different period ranges. ***Sa<sub>avg2</sub>***:  $0.2 T$ - $2 T$ ; ***Sa<sub>avg3</sub>***:  $0.2 T$ - $3 T$ . Period range: 0.1 s to 4 s.
- ***FIV3(T)***: filtered incremental velocity, defined by Dávalos and Miranda (2019). Period range: 0.1 s to 4 s

*RotD50* for: *PGA*, *PGV*, *Sa*, and *Sa<sub>avg</sub>*

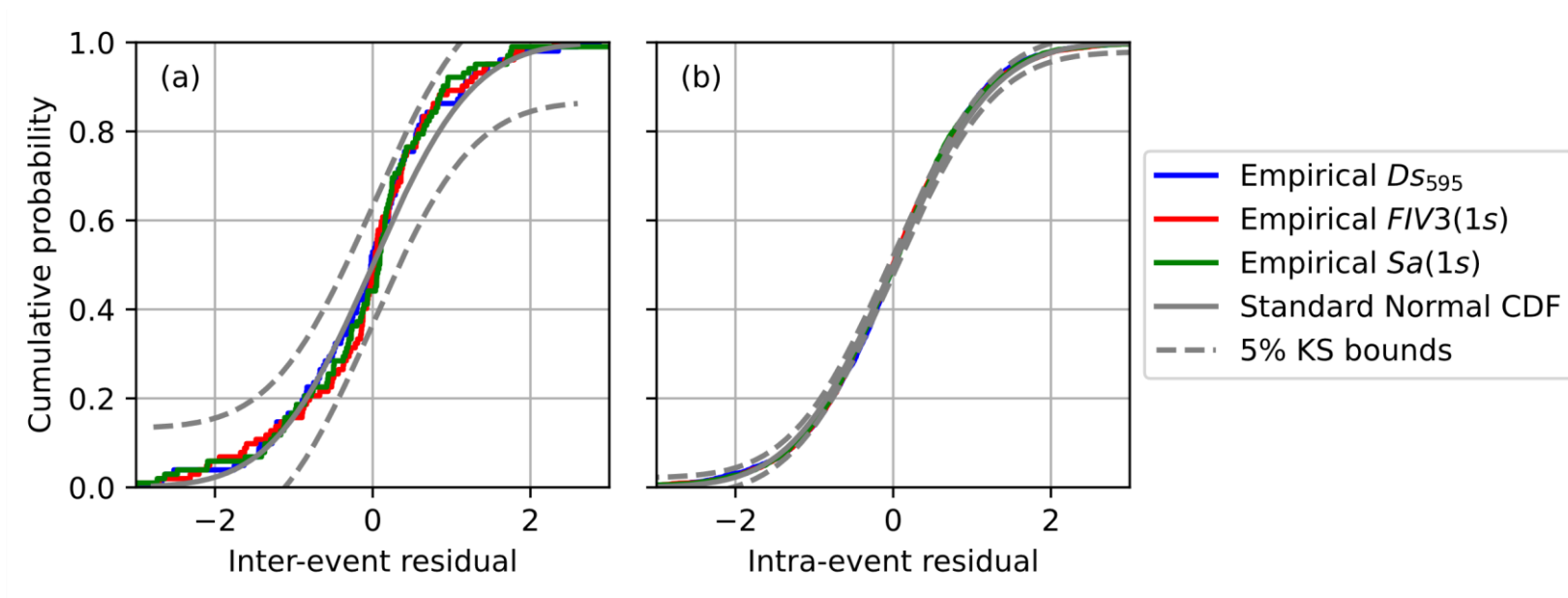
Geometric mean for: *Ds* and *FIV3*

Total of 24 cross-correlation models

| IM <sub>i</sub> \ IM <sub>j</sub> | <i>Sa</i>                | <i>Sa<sub>avg2</sub></i>           | <i>Sa<sub>avg3</sub></i>           | <i>PGA</i>  | <i>PGV</i>  | <i>Ds<sub>575</sub></i> | <i>Ds<sub>595</sub></i> | <i>FIV3</i> |
|-----------------------------------|--------------------------|------------------------------------|------------------------------------|-------------|-------------|-------------------------|-------------------------|-------------|
| <i>Sa</i>                         | ASO24, BJ08, ASA14, BB17 | ASO24, CB14 & BJ08*, CB14 & ASA14* | ASO24, CB14 & BJ08*, CB14 & ASA14* | BB17, TBB23 | BB17, TBB23 | ASO24, B11, BB17        | ASO24, B11, BB17        | ASO24       |
| <i>Sa<sub>avg2</sub></i>          |                          | ASO24                              | ASO24                              | ASO24       | ASO24       | ASO24                   | ASO24                   | ASO24       |
| <i>Sa<sub>avg3</sub></i>          |                          |                                    | ASO24, DM21                        | ASO24       | ASO24       | ASO24                   | ASO24                   | ASO24       |
| <i>PGA</i>                        |                          |                                    |                                    |             | BB17, TBB23 | BB17, TBB23, B11        | BB17, TBB23, B11        | ASO24       |
| <i>PGV</i>                        |                          |                                    |                                    |             |             | BB17, TBB23, B11        | BB17, TBB23, B11        | ASO24       |
| <i>Ds<sub>575</sub></i>           |                          |                                    |                                    |             |             |                         | BB17, TBB23, B11        | ASO24       |
| <i>Ds<sub>595</sub></i>           |                          |                                    |                                    |             |             |                         |                         | ASO24       |
| <i>FIV3</i>                       |                          |                                    |                                    |             |             |                         |                         | ASO24       |

# Database and ground motion model

- Single generalised ground motion model (GGMM) was used: Aristeidou et al. (2024) – ASO24
- NGA-West2 database, with the same filtering criteria as ASO24
- 4,135 ground motion records from 102 earthquakes
- Empirical distributions of normalised inter- and intra-event residuals are shown in the figure below. They are compared with the Kolmogorov-Smirnov (KS) goodness-of-fit bounds at 5% significant level



# Methodology

- From the GMM and filtered ground motion database
- Residuals are computed for each record

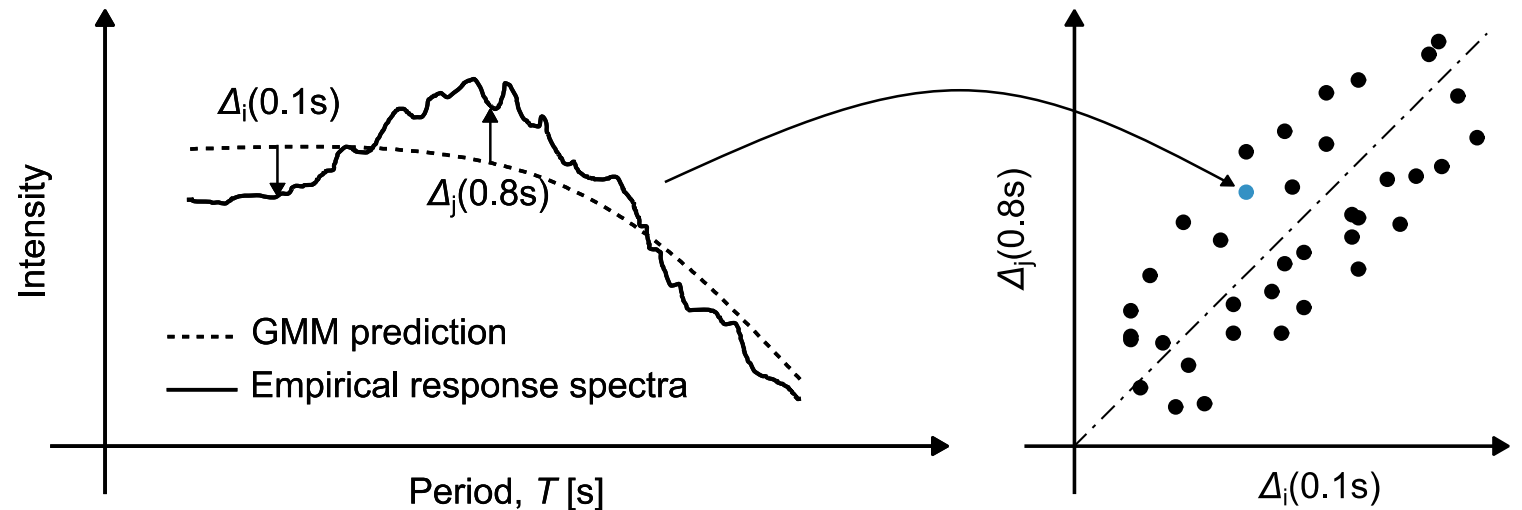
$$\log_{10} IM_i = f_i(\mathbf{X}, \boldsymbol{\theta}) + \delta b_i \tau_i + \delta w_i \varphi_i$$

$$\delta_i \sigma_i = \delta b_i \tau_i + \delta w_i \varphi_i$$

$$\delta_{i,g} = \frac{\log_{10} IM_{i,g} - \mu_{\log_{10} IM_i | \mathbf{X}, \boldsymbol{\theta}}}{\sigma_i}$$

$$\rho_{\delta_i, \delta_j} = \frac{\rho_{\delta b_i, \delta b_j} \tau_i \tau_j + \rho_{\delta w_i, \delta w_j} \varphi_i \varphi_j}{\sigma_i \sigma_j}$$

$$\rho_{\log_{10} IM_i | \mathbf{X}, \boldsymbol{\theta}, \log_{10} IM_j | \mathbf{X}, \boldsymbol{\theta}} = \rho_{\delta_i, \delta_j}$$



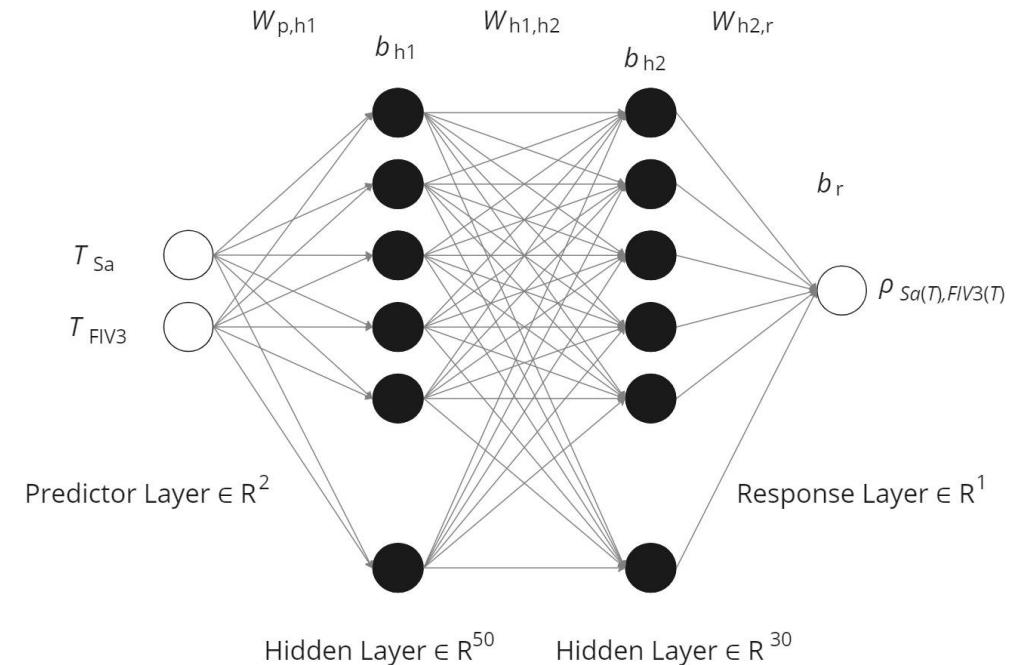
# Artificial neural network architecture

- Empirical correlation coefficient regressed with ANN
- ANN has the advantage of not needing predefined analytical functions
- It minimises the misfit between observed and predicted values
- Optimal hyperparameters for each model were chosen

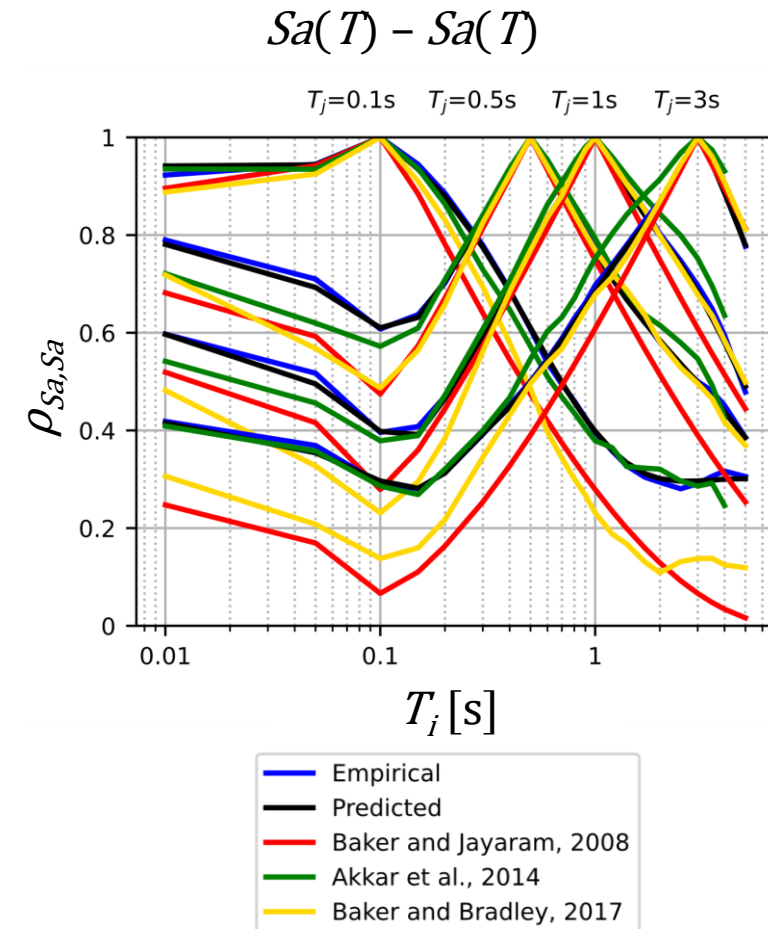
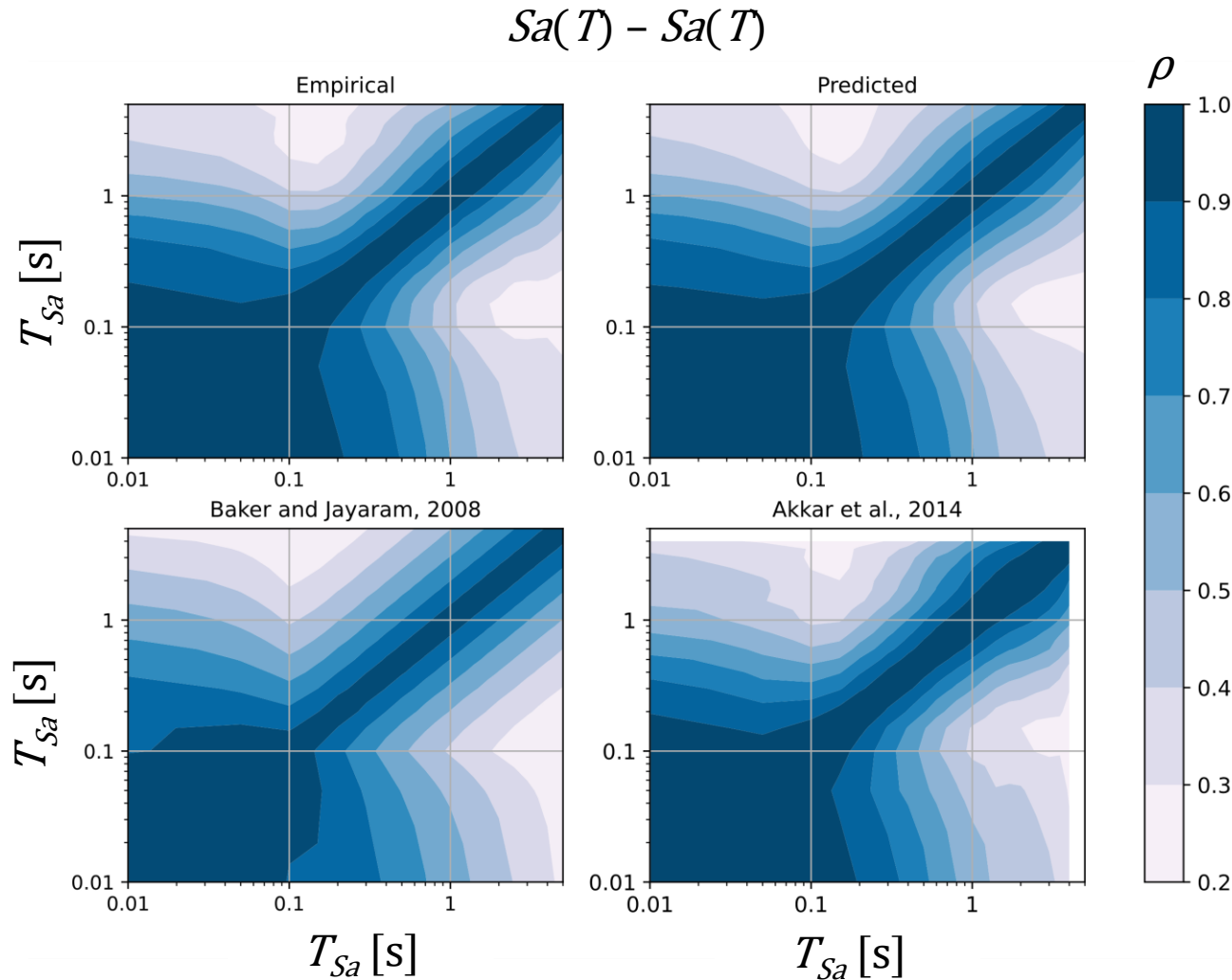
Correlation between an  $IM_i$ - $IM_j$  pair for the case of one hidden layer:

$$\rho_{\log_{10} IM_i, \log_{10} IM_j} = f_{activation2} \left[ b_r + \sum_{h=1}^{n_h} W_{h,r} \cdot f_{activation1} \left( b_h + \sum_{p=1}^{n_p} W_{p,h} X_p \right) \right]$$

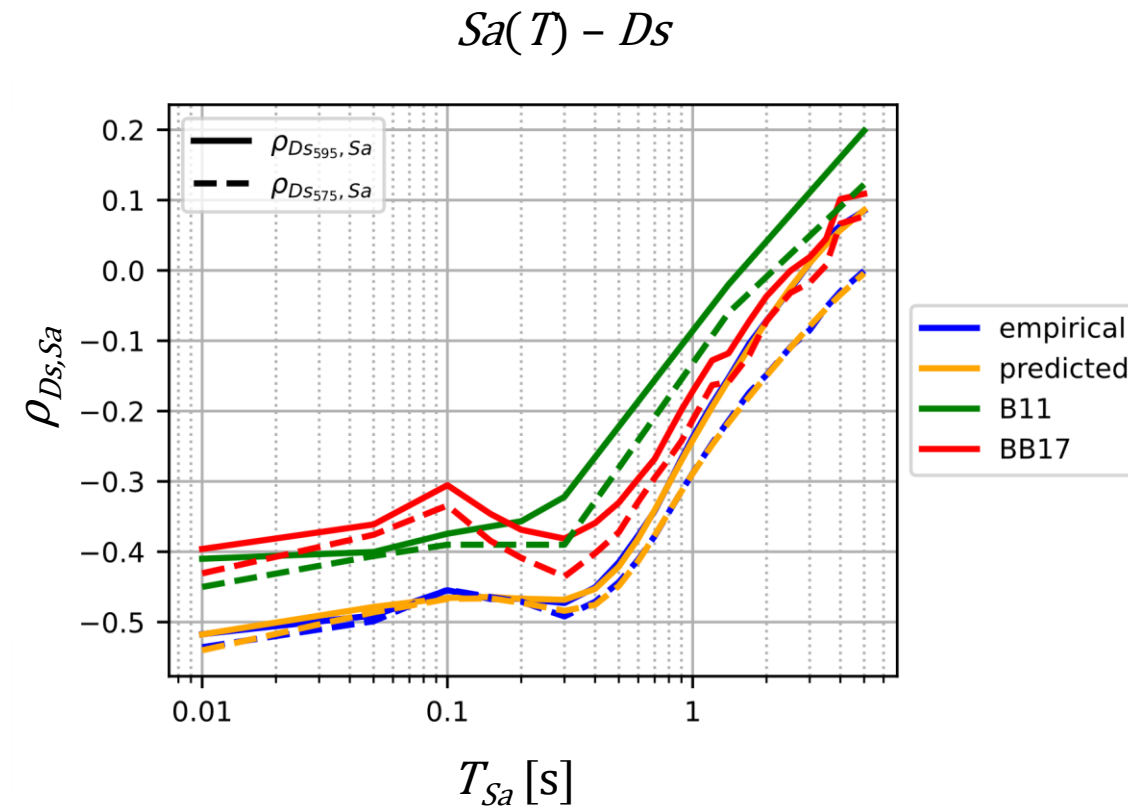
Schematic representation of the network for the case of *Sa-FIV3* correlation model:



# Results – Correlations between traditional IMs

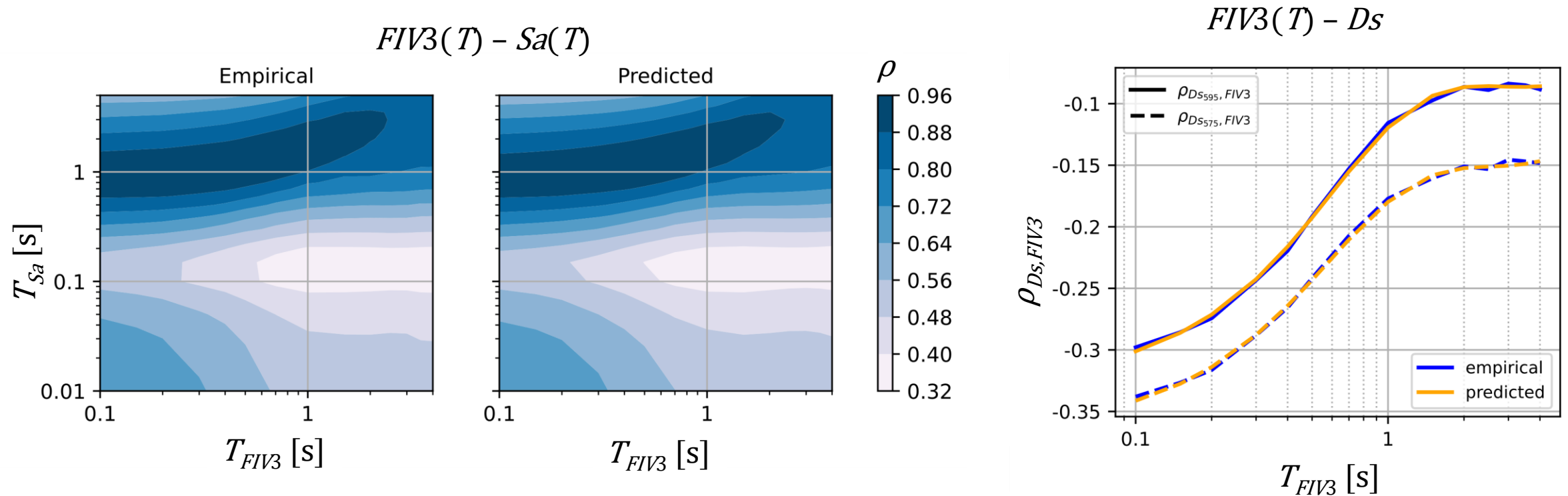


# Results – Correlations between traditional IMs

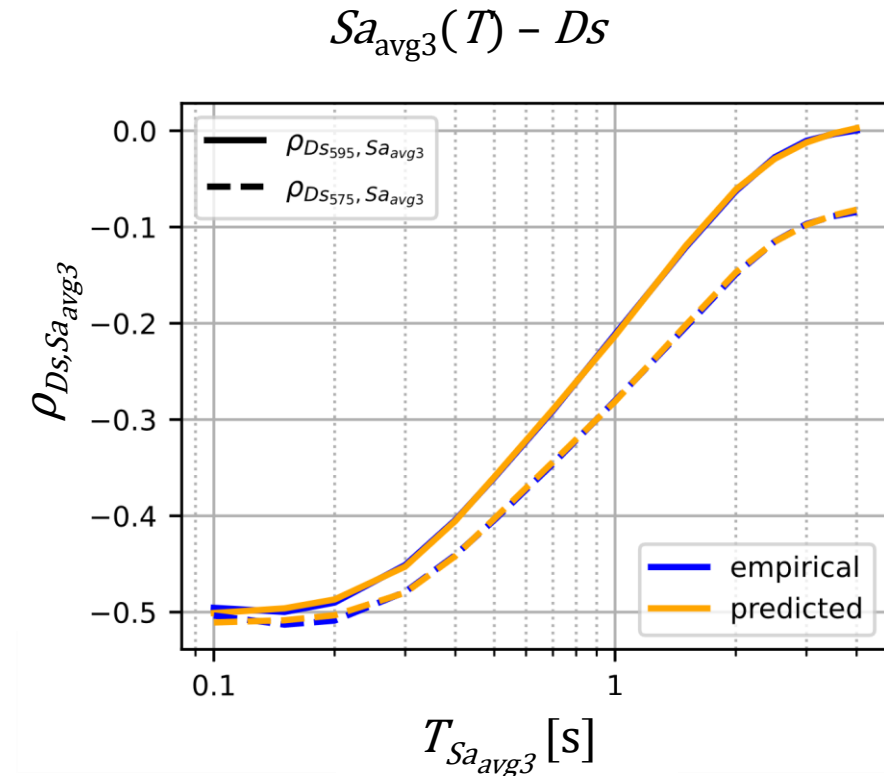
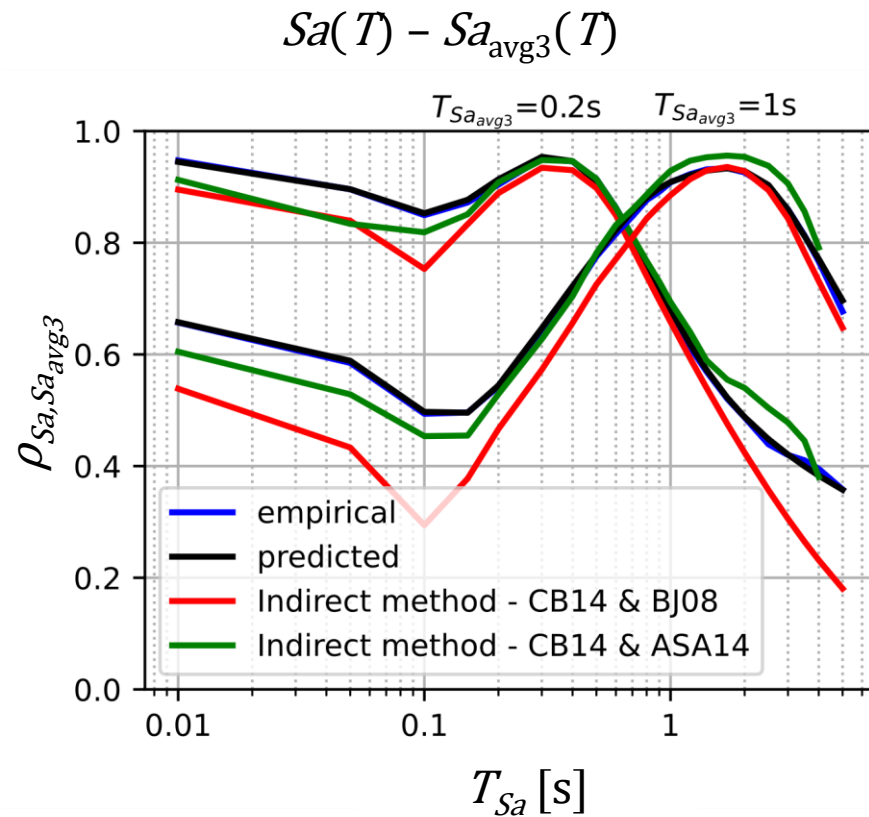




# Results – Correlations between traditional and next-generation IMs

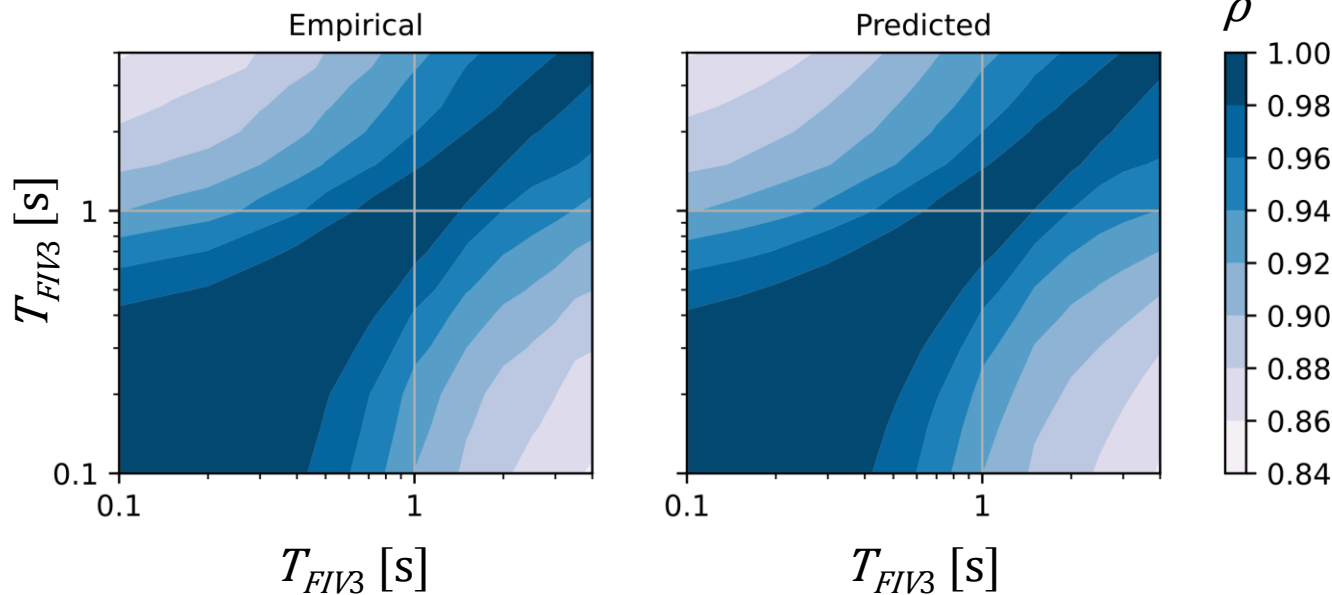


# Results – Correlations between traditional and next-generation IMs

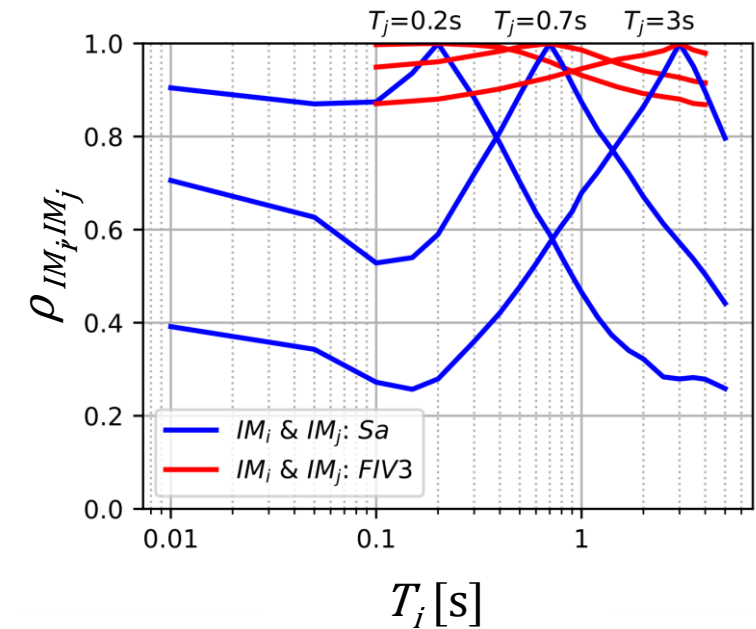


# Results – Correlations between next-generation IMs

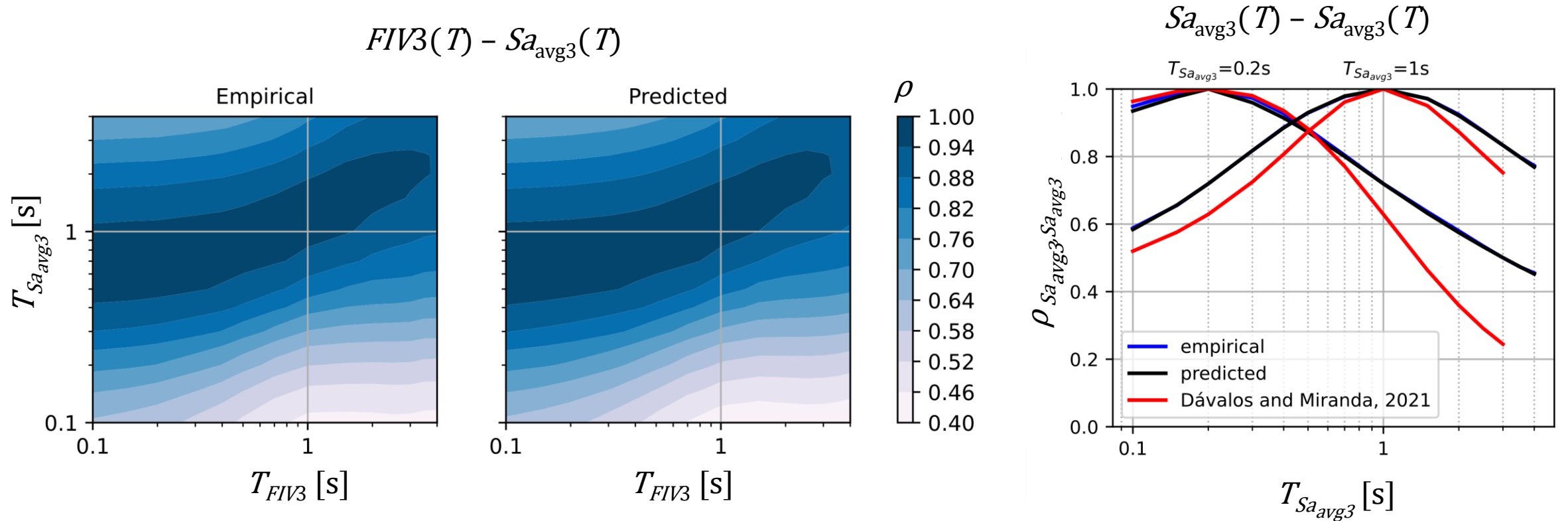
$FIV3(T) - FIV3(T)$



$Sa(T) - Sa(T) \text{ \& } FIV3(T) - FIV3(T)$



# Results – Correlations between next-generation IMs



# Discussion and conclusions

- This study presented the empirical correlations between miscellaneous IMs finding use in contemporary risk analyses (24 IM pairs in total)
- Regarding *FIV3*:
  - Strongly correlated with  $Sa(T=0.6-3s)$
  - Very well correlated with itself across all periods
  - Weak negative correlation with duration at short periods and near-zero correlation at longer periods
  - $Ds - FIV3$  has similar trend with  $Ds - Sa$ , but with a slightly weaker negative correlation (i.e., taking values closer to 0)
  - $FIV3 - Sa_{avg}$  very similar with  $FIV3 - Sa$
- Direct correlation of  $Sa_{avg}$  with itself and other IMs → allowing for a more consistent ground motion record selection, rather than the indirect method
- Predictive models based on regression with ANN. Has not been used before for fitting IM cross-correlation models
- The procedure adopted and the network architecture can be seamlessly adapted to develop correlation models for other IMs and/or horizontal component definitions

Aristeidou, S., Shahnazaryan, D. and O'Reilly, G.J. (2024) 'Correlation Models for Next-Generation Amplitude and Cumulative Intensity Measures using Artificial Neural Networks', Earthquake Spectra (Accepted)

Thank you!



Questions?



Correlations models are available to use at:

[https://github.com/Savvinos-Aristeidou/ANN\\_correlation\\_models.git](https://github.com/Savvinos-Aristeidou/ANN_correlation_models.git)



Soon to be implemented in OpenQuake



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